國立中央大學數學系 專題演講

主 講 人:鄭堯助理教授(淡江大學應用數學與數據科學學系)

演講題目: ON REPRESENTATIONS OF $Mp_2(E)$ DISTINGUISHED BY $SL_2(F)$

演講茶會: 2025年11月20日(星期四) 15:30~16:00

茶會地點:中央大學鴻經館M306

演講時間:2025年11月20日(星期四)16:00~17:00

演講地點:中央大學鴻經館M107

Abstract:

ABSTRACT. Let G be a group and H be its subgroup. Given irreducible representations π of G and σ of H, the restriction problem in the representation theory concerns the following problems:

(1) When does $\operatorname{Hom}_H(\pi|_H, \sigma) \neq 0$?

(2) If $\operatorname{Hom}_H(\pi|_H, \sigma) \neq 0$, what is its dimension?

When σ is the trivial representation of H, restriction problem is also known as distinction problem (hence the title).

When G is finite or a compact classical groups, these problems have satisfactory answers in the literature. More recently, the celebrated Gan-Gross-Prasad conjecture proposes conjectural answers to restriction problems for a more general class of classical groups, including those over p-adic fields. Their conjecture has been settled in many cases, and the study of restriction problems remains very active in representation theory.

In a recent joint work with Hsin-Yen Ho and Hao-An Wu, we consider the case that is not covered in their conjecture, and obtained satisfactory answers. More concretely, let E/F be a quadratic extension of p-adic fields, and let $\operatorname{Mp}_2(E)$ denote the non-trivial twofold cover of $\operatorname{SL}_2(E)$. The group $\operatorname{SL}_2(F)$ embeds into $\operatorname{Mp}_2(E)$ naturally, and we study the distinction problem for

$$(G, H) = (\mathrm{Mp}_2(E), \mathrm{SL}_2(F)),$$

 π a genuine representation of $\mathrm{Mp}_2(E)$, and σ the trivial representation of $\mathrm{SL}_2(F)$.

In this talk, I will present our results and explain how we obtained them.